## Worksheet 1 - lines and tangent lines

If you had trouble with question 1, do these problems.

1. Find the line through the points (3,0) and (0,2).

Method 1: If the slope is m, and the point  $(x_0, y_0)$  is on the line, one equation for the line is

$$y - y_0 = m(x - x_0).$$

Method 2: Cool fact: the line through (a, 0) and (0, b) can be written x/a + y/b = 1.

- 2. Find an equation for the line through (4,0) and (0,-5).
- 3. Find an equation for the line through the points (1, 1) and (4, 5) using the first method.
- 4. Graph the lines x + y = 1 and y x = 1.
- 5. Suppose that a right triangle has vertices (0,0), (0,10), and (4,0). How wide across is the triangle at height y = 3?
- 6. Find the equation of the tangent line to  $f(x) = x^2$  at x = 1.
- 7. Plug x = 1.1 into your tangent line from the last problem. How close is the resulting y value to f(1.1)? Is the tangent line a good approximation to the curve near x = 1?
- 8. For which values of x does the tangent line approximation in the previous problem have error less than 1/10?